



On Generalized Degree Fairness in Graph Neural Networks

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Code: <https://github.com/ntkien1904/DegFairGNN>

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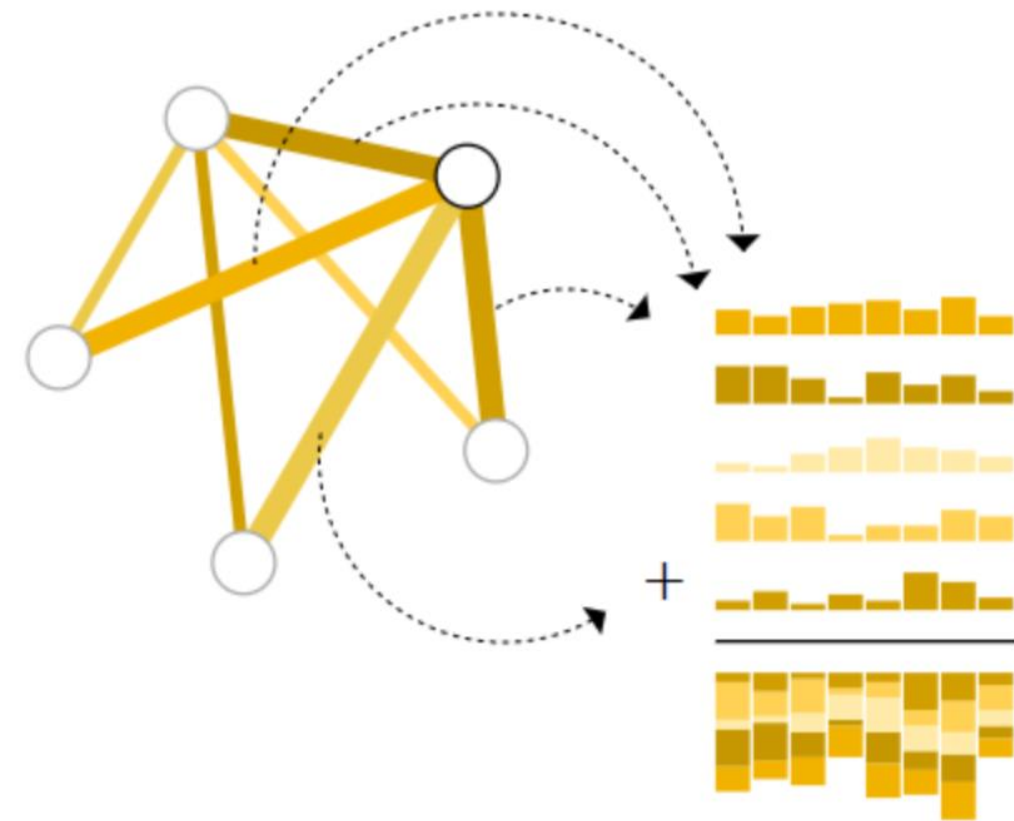
Reported by Renhui Luo



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Introduction



Conventional graph neural networks (GNNs) confronted with fairness issues that may stem from their input, including node attributes and neighbors surrounding a node.

Existing studies have shown that the structure of graph neural networks can further strengthen the biases hidden in data, thus leading to discriminatory decisions regarding age, gender, race, etc

GNN , aggregate information from adjacent nodes



Introduction

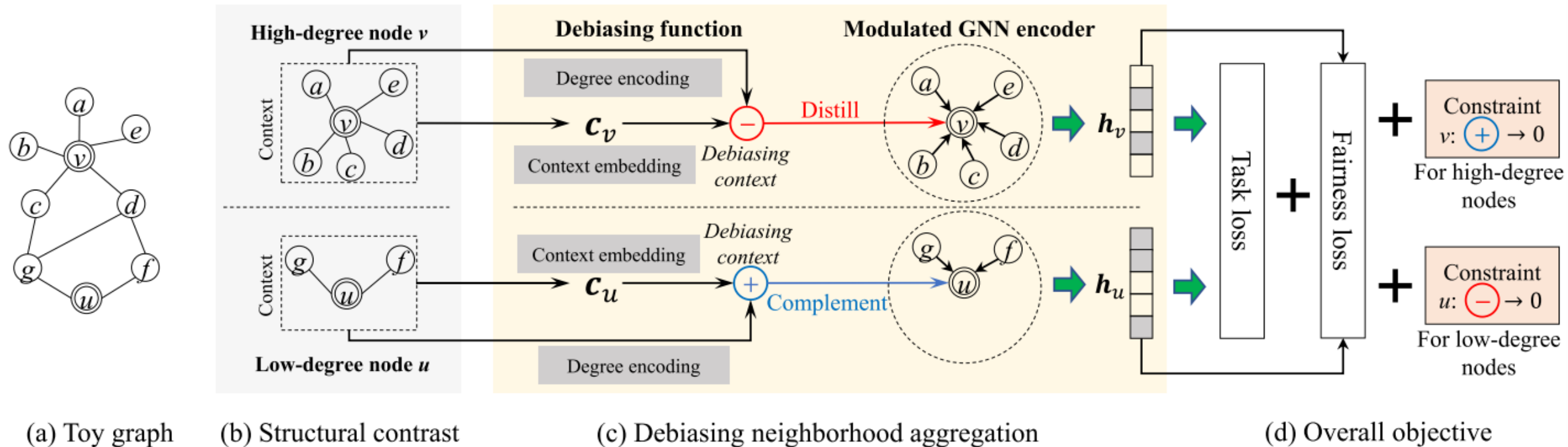
QUESTION:

1. drastic differences in node degrees could lead to differential node behaviors and biased outcomes.
2. a node of larger degree is more likely to possess crucial advantages and thus receives more favorable outcomes than warranted.

WORK:

1. Defining and addressing generalized degree fairness in GNNs.
2. DegFairGNN that can flexibly work with neighborhood aggregation-based GNNs, to eliminate the generalized degree bias rooted in the layer-wise neighborhood aggregation.

Overview



Method

Generalized degree

$$\text{deg}_r(v) = [\mathbf{A}^r \mathbf{1}]_v, \quad (1)$$

Generalized degree fairness

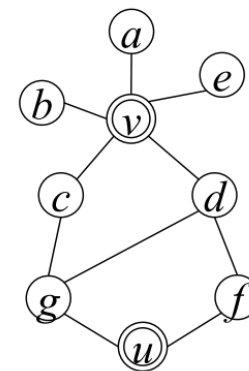
$$\mathcal{G}_i = \{v \in \mathcal{V} \mid d_i \leq \text{deg}_r(v) < d_{i+1}\}, \quad (2)$$

Degree Statistical Parity (DSP)

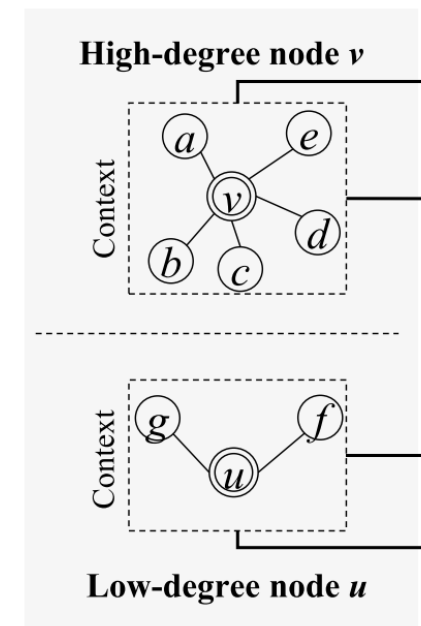
$$P(\hat{y}_v = y \mid v \in \mathcal{G}_i) = P(\hat{y}_v = y \mid v \in \mathcal{G}_j), \quad (3)$$

Degree Equal Opportunity (DEO)

$$P(\hat{y}_v = y \mid y_v = y, v \in \mathcal{G}_i) = P(\hat{y}_v = y \mid y_v = y, v \in \mathcal{G}_j).$$

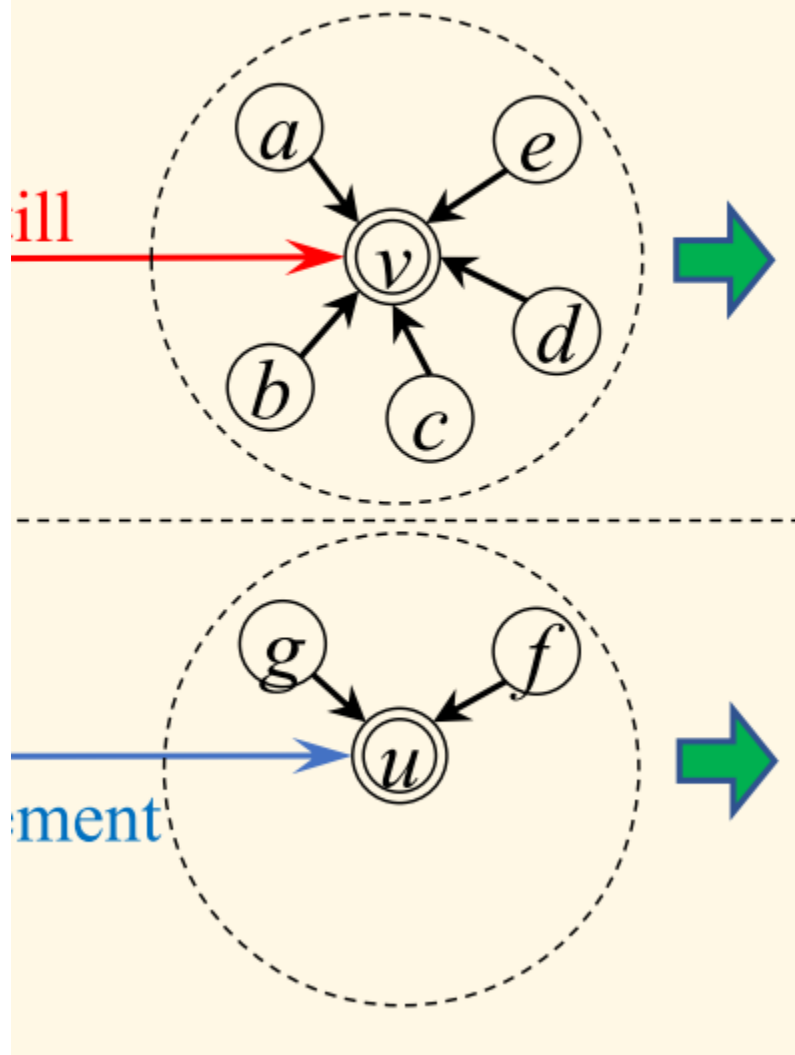


(a) Toy graph



(b) Structural contrast

Modulated GNN encoder

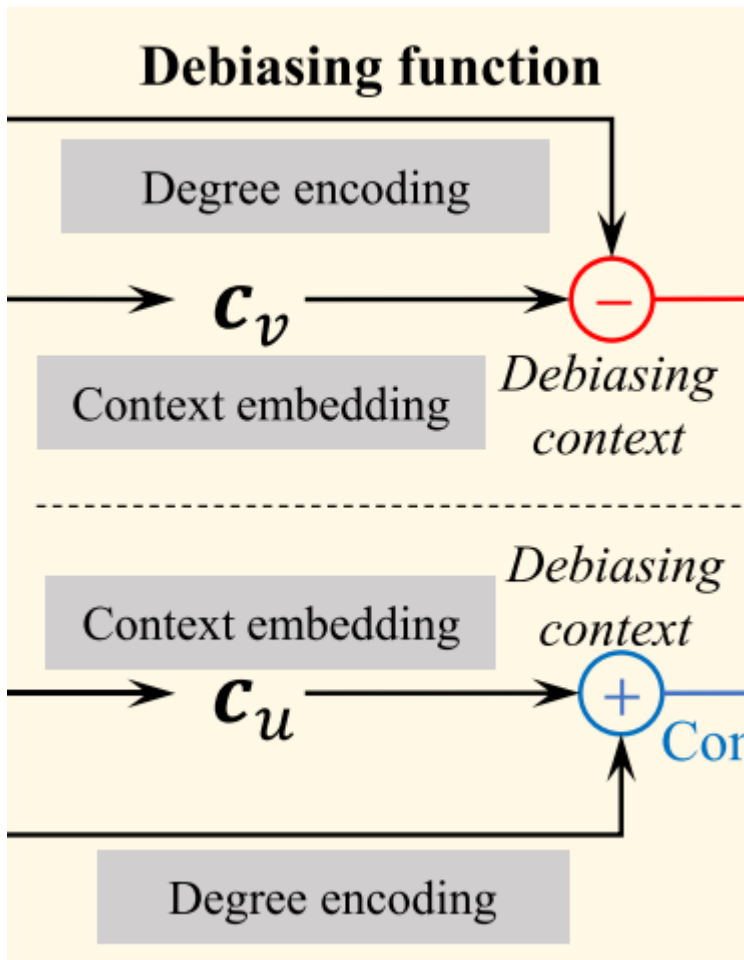


Method

$$\mathbf{h}_v^l = \sigma \left(\text{AGGR} \left(\{ \mathbf{h}_u^{l-1} \mid u \in \mathcal{N}_v \}; \omega^l \right) \right), \quad (4)$$

$$\mathbf{h}_v^l = \sigma \left(\text{AGGR} \left(\{ \mathbf{h}_u^{l-1} \mid u \in \mathcal{N}_v \}; \omega^l \right) + \epsilon \cdot \left(\underbrace{I(v \in \mathcal{S}_0) \mathcal{D}(v; \theta_0^l)}_{\text{complement low-deg. group}} + \underbrace{I(v \in \mathcal{S}_1) \mathcal{D}(v; \theta_1^l)}_{\text{distill high-deg. group}} \right) \right), \quad (9)$$

Method



Comprehensiveness

$$\mathbf{c}_v^l = \text{POOL}(\{\mathbf{h}_u^{l-1} \mid u \in \mathcal{C}_r(v)\}), \quad (5)$$

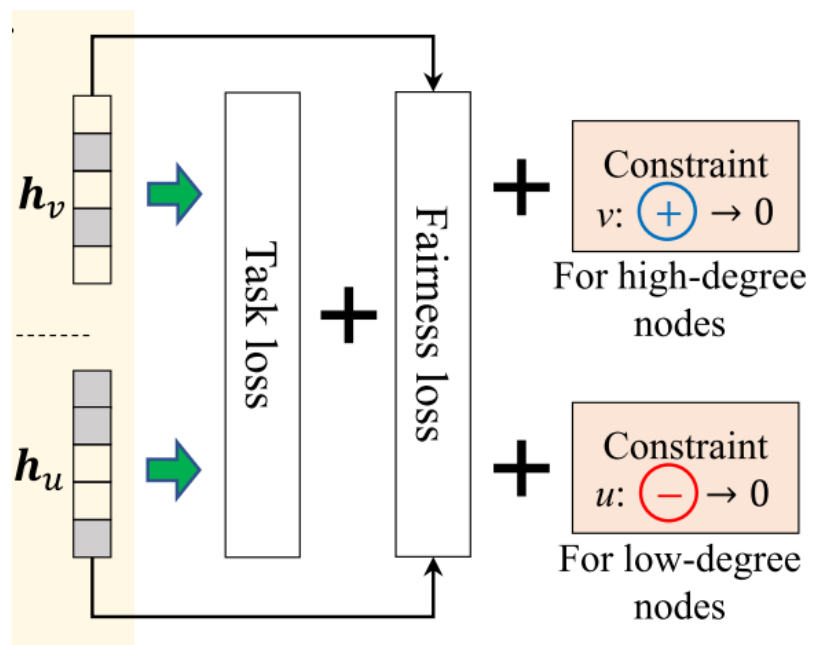
$$\mathcal{D}(v; \theta_*^l) = f(\mathbf{c}_v^l; \theta_{c,*}^l), \quad (6)$$

Adaptiveness

$$\mathcal{D}(v; \theta_*^l) = (\gamma_v^l + \mathbf{1}) \odot f(\mathbf{c}_v^l; \theta_{c,*}^l) + \beta_v^l, \quad (7)$$

$$\gamma_v^l = \phi_\gamma(\delta^l(v); \theta_\gamma^l), \quad \beta_v^l = \phi_\beta(\delta^l(v); \theta_\beta^l), \quad (8)$$

Method



(d) Overall objective

Classification loss

$$\mathcal{L}_1 = - \sum_{v \in \mathcal{V}^{\text{tr}}} \sum_{y=1}^{|\mathcal{Y}|} [\mathbf{y}_v]_y \ln[\mathbf{h}_v^\ell]_y, \quad (10)$$

Fairness loss

$$\mathcal{L}_2 = \left\| \frac{1}{|\mathcal{S}_0^{\text{tr}}|} \sum_{v \in \mathcal{S}_0^{\text{tr}}} \mathbf{h}_v^\ell - \frac{1}{|\mathcal{S}_1^{\text{tr}}|} \sum_{v \in \mathcal{S}_1^{\text{tr}}} \mathbf{h}_v^\ell \right\|_2^2, \quad (11)$$

Constraints on debiasing contexts

$$\mathcal{L}_3 = \sum_{l=1}^{\ell} \left(\sum_{v \in \mathcal{S}_0^{\text{tr}}} \|\mathcal{D}(v; \theta_1^l)\|_2^2 + \sum_{v \in \mathcal{S}_1^{\text{tr}}} \|\mathcal{D}(v; \theta_0^l)\|_2^2 \right). \quad (12)$$

Constraints on scaling and shifting

$$\mathcal{L}_4 = \sum_{l=1}^{\ell} \sum_{v \in \mathcal{V}^{\text{tr}}} (\|\gamma_v^l\|_2^2 + \|\beta_v^l\|_2^2). \quad (13)$$

Overall loss

$$\mathcal{L} = \mathcal{L}_1 + \mu \mathcal{L}_2 + \lambda (\mathcal{L}_3 + \mathcal{L}_4), \quad (14)$$

Experiments

Table 2: Comparison with baselines ($r = 1$, 20% Top/Bottom).Henceforth, tabular results are in percent with standard deviation over 5 runs; the best fairness result is **bolded** and the runner-up is underlined.

		GCN	DSGCN	Residual2Vec	Tail-GNN	FairWalk	CFC	FairGNN	FairAdj	FairVGNN	DegFairGCN
Chamel.	Acc. \uparrow	62.45 \pm 0.21	63.90 \pm 1.28	49.04 \pm 0.01	66.08 \pm 0.19	56.36 \pm 0.75	63.02 \pm 0.84	70.70 \pm 0.52	51.71 \pm 1.13	72.32 \pm 0.50	69.91 \pm 0.19
	Δ_{DSP} \downarrow	9.68 \pm 1.37	8.81 \pm 1.15	14.52 \pm 0.69	8.51 \pm 1.72	8.18 \pm 0.93	10.12 \pm 1.28	<u>7.33</u> \pm 1.09	9.79 \pm 1.91	8.86 \pm 1.11	5.85 \pm 0.32
	Δ_{DEO} \downarrow	36.08 \pm 2.65	25.14 \pm 2.67	37.31 \pm 1.99	26.09 \pm 3.25	<u>22.89</u> \pm 2.75	29.54 \pm 1.95	26.83 \pm 1.95	27.48 \pm 2.06	26.02 \pm 2.39	21.60 \pm 0.71
Squirrel	Acc. \uparrow	47.85 \pm 1.33	40.71 \pm 2.17	28.47 \pm 0.01	42.62 \pm 0.06	37.68 \pm 0.65	45.64 \pm 2.19	57.29 \pm 0.77	35.18 \pm 1.22	46.97 \pm 0.48	59.21 \pm 0.97
	Δ_{DSP} \downarrow	13.37 \pm 2.83	16.08 \pm 0.86	25.11 \pm 0.48	18.91 \pm 0.26	7.94 \pm 0.36	12.40 \pm 0.48	12.96 \pm 1.03	16.63 \pm 1.56	26.67 \pm 0.52	<u>9.54</u> \pm 1.02
	Δ_{DEO} \downarrow	27.00 \pm 3.79	32.61 \pm 3.74	34.49 \pm 0.72	33.60 \pm 0.72	<u>17.12</u> \pm 1.50	21.60 \pm 2.69	17.62 \pm 2.40	27.54 \pm 1.73	35.80 \pm 1.76	16.42 \pm 1.38
EMNLP	Acc. \uparrow	78.92 \pm 0.43	82.19 \pm 0.77	80.69 \pm 0.01	83.72 \pm 0.28	82.23 \pm 0.18	80.15 \pm 1.13	86.81 \pm 0.22	76.50 \pm 1.55	84.03 \pm 0.34	79.92 \pm 0.77
	Δ_{DSP} \downarrow	44.55 \pm 1.90	50.00 \pm 2.98	<u>12.90</u> \pm 0.15	41.18 \pm 1.58	33.52 \pm 1.46	56.60 \pm 1.95	58.23 \pm 1.44	40.38 \pm 4.64	43.92 \pm 1.43	12.38 \pm 3.72
	Δ_{DEO} \downarrow	34.05 \pm 3.56	46.92 \pm 2.91	<u>11.26</u> \pm 0.67	36.76 \pm 1.48	30.67 \pm 1.42	45.21 \pm 2.27	51.56 \pm 1.38	41.89 \pm 4.78	40.95 \pm 1.71	8.52 \pm 2.26

Experiments

Table 3: Comparison to baselines ($r = 2$, 20% Top/Bottom).

		GCN	FairWalk	FairGNN	DegFairGCN
Chamel.	Acc. \uparrow	62.45 ± 0.21	56.36 ± 0.75	70.70 ± 0.52	69.91 ± 0.19
	$\Delta_{\text{DSP}} \downarrow$	5.96 ± 0.89	10.38 ± 0.85	6.70 ± 0.32	5.25 ± 0.39
	$\Delta_{\text{DEO}} \downarrow$	26.92 ± 2.09	25.46 ± 1.66	23.66 ± 0.93	19.05 ± 0.74
Squirrel	Acc. \uparrow	47.85 ± 1.33	37.68 ± 0.65	57.29 ± 0.77	59.21 ± 0.97
	$\Delta_{\text{DSP}} \downarrow$	14.61 ± 2.63	9.64 ± 0.50	11.11 ± 0.93	8.26 ± 0.57
	$\Delta_{\text{DEO}} \downarrow$	28.62 ± 3.89	17.37 ± 1.10	16.29 ± 2.07	14.95 ± 1.22
EMNLP	Acc. \uparrow	78.92 ± 0.43	82.23 ± 0.18	86.81 ± 0.22	79.92 ± 0.77
	$\Delta_{\text{DSP}} \downarrow$	45.03 ± 1.77	34.80 ± 1.26	52.88 ± 1.39	10.87 ± 4.00
	$\Delta_{\text{DEO}} \downarrow$	34.71 ± 3.31	31.11 ± 1.34	45.78 ± 1.36	8.72 ± 2.17

Table 4: Comparison to baselines ($r = 1$, 30% Top/Bottom).

		GCN	FairWalk	FairGNN	DegFairGCN
Chamel.	Acc. \uparrow	62.45 ± 0.21	56.36 ± 0.75	70.70 ± 0.52	69.91 ± 0.19
	$\Delta_{\text{DSP}} \downarrow$	5.95 ± 1.02	8.16 ± 0.38	6.92 ± 0.29	4.15 ± 0.02
	$\Delta_{\text{DEO}} \downarrow$	18.00 ± 1.76	16.65 ± 1.32	14.52 ± 1.09	8.39 ± 0.37
Squirrel	Acc. \uparrow	47.85 ± 1.33	37.68 ± 0.65	57.29 ± 0.77	59.21 ± 0.97
	$\Delta_{\text{DSP}} \downarrow$	10.34 ± 2.15	6.17 ± 0.36	9.27 ± 0.68	7.39 ± 0.63
	$\Delta_{\text{DEO}} \downarrow$	22.62 ± 3.10	14.97 ± 1.12	17.42 ± 1.11	17.71 ± 1.05
EMNLP	Acc. \uparrow	78.92 ± 0.43	82.23 ± 0.18	86.81 ± 0.22	79.92 ± 0.77
	$\Delta_{\text{DSP}} \downarrow$	42.87 ± 1.40	34.19 ± 0.91	48.25 ± 1.97	14.46 ± 3.35
	$\Delta_{\text{DEO}} \downarrow$	37.89 ± 3.27	34.49 ± 0.91	48.83 ± 1.97	10.92 ± 2.87

Experiments

 Table 5: With other base GNNs ($r = 1$, 20% Top/Bottom).

		GAT	DegFairGAT	GraphSAGE	DegFairSAGE
Chamel.	Acc. \uparrow	63.15 ± 0.40	69.64 ± 0.44	53.15 ± 0.56	60.95 ± 0.84
	$\Delta_{DSP} \downarrow$	9.35 ± 1.61	7.88 ± 1.30	10.86 ± 0.74	8.22 ± 1.22
	$\Delta_{DEO} \downarrow$	29.59 ± 1.43	26.12 ± 2.06	29.42 ± 1.57	26.40 ± 2.32
Squirrel	Acc. \uparrow	41.44 ± 0.21	45.55 ± 1.44	34.39 ± 0.62	34.63 ± 1.31
	$\Delta_{DSP} \downarrow$	12.60 ± 0.77	12.03 ± 0.63	5.39 ± 0.66	3.76 ± 0.23
	$\Delta_{DEO} \downarrow$	24.89 ± 0.69	20.64 ± 3.06	17.13 ± 2.86	14.91 ± 1.35
EMNLP	Acc. \uparrow	70.42 ± 0.77	81.57 ± 1.14	83.96 ± 0.31	83.57 ± 0.44
	$\Delta_{DSP} \downarrow$	24.40 ± 3.06	14.11 ± 6.28	56.33 ± 1.12	28.43 ± 3.79
	$\Delta_{DEO} \downarrow$	8.36 ± 1.29	12.28 ± 6.19	51.71 ± 0.88	24.65 ± 3.35

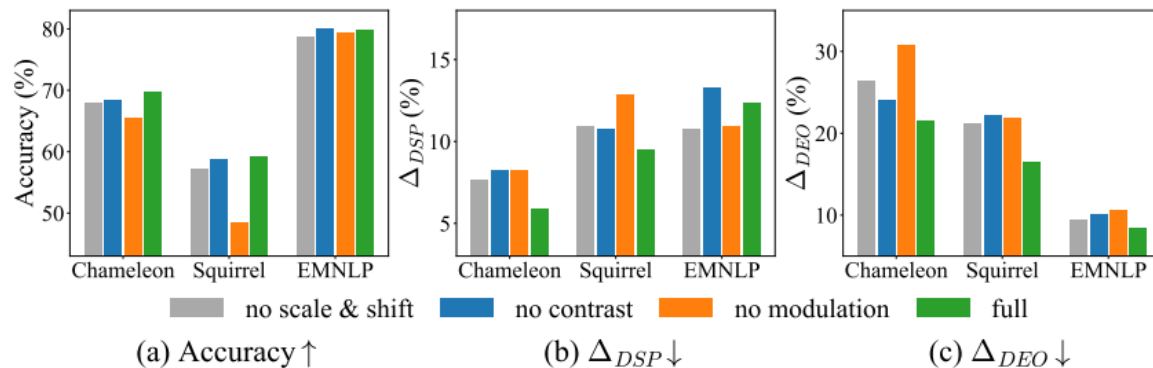


Figure 2: Ablation study on the effect of each module.



THANKS